P(III)-Physics-H-7A

2020

PHYSICS — HONOURS

Seventh Paper

(Group - A)

Full Marks : 50

The figures in the margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable.

Answer question no. 1 and any four questions from the rest.

1. Answer any five questions :

 2×5

- (a) State the postulate of classical statistical mechanics.
- (b) The description of the microcanonical ensemble is given in terms of N, V and the energy between E and $E + \Delta E$, $\Delta E \ll E$. Why do we need the spread ΔE in energy?
- (c) What is thermal wavelength?
- (d) Explain the physical significance of the Poynting Vector.
- (e) Show that the electric field vector can be written as $\overline{E} = -\overline{\nabla}\phi \frac{\partial A}{\partial t}$, in case of a time varying

electromagnetic field, where ϕ and \overline{A} are the scalar and vector potentials respectively.

- (f) Find an expression for velocity of light in terms of permittivity and permeability starting from Maxwell's equations.
- 2. (a) State the theorem of equipartition of energy and derive its mathematical expression.
 - (b) Find the average energy (using the above theorem) of a system of N ideal monatomic molecules. (2+5)+3
- 3. In how many ways *n* fermions can be distributed among *g* non-degenerate levels? Obtain the Fermi-Dirac distribution function at a temperature *T* using the Boltzmann relation for entropy $S = k \log W$, where the symbols have their usual meanings. Obtain an expression for electronic specific heat for metals at low temperature. 2+4+4
- 4. Starting from Planck's law for black body radiation, show that the emissive power of a black body is proportional to the fourth power of its absolute temperature. You may use the following results.

$$\int_{0}^{\infty} \frac{x^{3}}{e^{x} - 1} dx = \frac{\pi^{4}}{15}$$

Please Turn Over

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A spherical black body of radius 1cm is enclosed in a evacuated chamber. If the chamber is at a temperature 300K, find out the amount of heat that must be supplied per second to the black body to keep it at a temperature 1000K. Neglect conduction of heat. $(\sigma = 5.67 \times 10^{-8} W/m^2/K^4)$ 5+5

- 5. In a current free region $B_x = ax + bz$ and $B_y = ax + cy$. Find B_z assuming all currents are outside and $\vec{\nabla} \cdot \vec{j} = 0$. Obtain the reflection coefficient for normal incidence for an electromagnetic wave. Calculate the reflection coefficient for an electromagnetic wave of frequency 10 GHz when it is incident normally on a metal surface of conductivity $6 \times 10^7 (\Omega m)^{-1}$. Take $\epsilon \approx \epsilon_0$ and $\mu \approx \mu_0$. What is Brewster's angle? 2+4+2+2
- 6. Consider free electrons in a conductor not bound to any particular atom. Under the action of the field $E = E_0 e^{-i\omega t}$ with the charge 'q', mass 'm', ' γ ' the damping constant and 'f' the number of free electrons per atom, write down
 - (a) the equation of motion of the electrons
 - (b) solution of the equation
 - (c) an expression for the current J
 - (d) expression for real part of J
 - (e) physical significance of J being complex
 - (f) expression for the conductivity σ .
- 7. Starting with the Lorentz force law

$$\overline{F} = \frac{d\overline{p}}{dt} = q\left(\overline{E} + \overline{V} \times \overline{B}\right)$$

- (a) Write down \vec{F} using the vector and scalar potentials.
- (b) Show that $\frac{d\vec{A}}{dt} = \frac{\partial\vec{A}}{\partial t} + (\vec{V} \cdot \vec{\nabla})\vec{A}$.
- (c) Show that $\frac{d}{dt}\vec{p}_{canonical} = -\vec{\nabla}U$, where $\vec{p}_{canonical} = \vec{p} + q\vec{A}$ and $U = q(\phi \vec{V} \cdot \vec{A})$. 2+2+(3+3)

1+2+2+1+2+2